

CS 692 Capstone Exam Algorithms Fall 2019: Choose any 2 of the 3 problems.

1) Consider the implementation of a closed hash table  $a[0]..a[n-1]$  to store distinct positive integers, using quadratic probing to resolve collisions. A value of 0 indicates that a hash table location is currently unused. The hash function is  $h(x) = x \% n$ .

3) For each function with input argument  $n$ , determine the asymptotic number of “fundamental









# Theory Exam

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Answer \_\_\_\_\_ of the following three questions:

1. Give a context-free grammar generating the following language over  $\Sigma = \{0, 1\}$ :

$$\{0^m 1^n 0^k : k \leq m; m, n, k \geq 0\}$$

2. A *Hamiltonian circuit* in an undirected graph is a cycle that visits each node exactly once. A *cycle* in a graph is a non-empty path in which the only repeated node is the first and last.

Consider the following problem:

$$C = \{V, E : G = (V, E) \text{ is an undirected graph containing a Hamiltonian circuit}\}$$

Show that  $C \in \text{NP}$ .

3. Answer \_\_\_\_\_ or \_\_\_\_\_  $\bar{m}H$

# SYSTEMS EXAM

Fall 2019

90 minutes

Check which problems you are submitting:

#1

#2

#3

How many pages total? \_

## Problem #1

a) (4pts) List the **four** conditions of **deadlock**:

b) (16pts) Below is a **semaphore** solution for the producer/consumer problem. The buffer can hold **n** items. Semaphores are X, Y , and Z.

```
// The buffer is initialized to be empty and is processed as a first in first out
// queue
```

```
// PRODUCER CODE
```

```
while (true)
```

```
{
```

1. getItem();
2. wait(X);
3. wait(Z);
4. addItemToBuffer();
5. signal(Z);
6. signal(Y);

```
}
```

```
// CONSUMER CODE
```

```
while(true)
```

```
{
```

1. wait(Y);
2. wait(Z);
3. readItemFromBuffer();
4. signal(Z);
5. signal(X);
6. processItem();

```
}
```

There is a problem with each of the semaphore initializations below. **Give a sequence of statements showing how an error might occur.**

For instance, can the Producer and Consumer be in their critical sections at the same time? Will deadlock occur?

Please note, for full credit, you must you must list a sequence of statements that lead to an error. You will not get credit for guessing.

- 1)  $X = 0, Y = 0, Z = 1$
- 2)  $X = n, Y = 0, Z = 0$
- 3)  $X = n, Y = 0, Z = 2$
- 4)  $X = 0, Y = n, Z = 1$

## Problem #2 Resource Allocation Banker's algorithm

safe state

(14pts) Show a **safe state process sequence** for the following:

Resources: X, Y, Z where available is  $X = 11, Y = 7, Z = 7$

	Allocated			Max			Need		
	X	Y	Z	X	Y	Z	X	Y	Z
P0	4	1	1	7	3	2	3	2	1
P1	3	1	2	5	2	7	2	1	5
P2	2	2	3	2	2	4	0	0	1
P3	2	2	0	4	4	1	2	2	1

(3pts) If a **P2** asks for **(3,2,4)** can it be granted? Why or why not?

